

# 2019 Ph H2 Q11

Section: Particles and Waves

Topic: Refraction, Critical Angle and Sparkle

(a) Light enters a diamond at  $49.0^\circ$ . Refractive index of diamond = 2.42. Calculate angle of refraction. (b) Calculate the critical angle of the diamond. (c) Moissanite has higher refractive index than diamond. Would it sparkle more or less than diamond? Justify.

## Worked solution

(a) Using Snell's law:  $n_1 \sin \theta_1 = n_2 \sin \theta_2$ .

Here  $n_1 = 1.00$  (air),  $n_2 = 2.42$ ,  $\theta_1 = 49.0^\circ$ .

$\sin \theta_2 = \sin(49.0^\circ)/2.42 = 0.312$ .

$\theta_2 = 18.2^\circ$ .

Answer:  $18.9^\circ$

(b) Critical angle  $c$  is given by  $\sin c = 1/n$ .

$= 1/2.42 = 0.413$ .

$c = 24.4^\circ$ .

Answer:  $24.4^\circ$

(c) A higher refractive index means a smaller critical angle. This increases the range of angles for total internal reflection, so more light is reflected inside the material and emerges later, enhancing sparkle.

Answer: Moissanite sparkles more than diamond.

## **Final answers**

**(a)  $\theta_2 = 18.9^\circ$**

**(b)  $c = 24.4^\circ$**

**(c) Moissanite sparkles more (smaller critical angle  $\rightarrow$  more TIR)**

## **Revision tips**

- Snell's Law:  $n_1 \sin\theta_1 = n_2 \sin\theta_2$ .
- Critical angle:  $\sin c = 1/n$ .
- Smaller critical angle  $\rightarrow$  more total internal reflection.
- Greater TIR  $\rightarrow$  more sparkle.
- Gemstones sparkle because of multiple internal reflections.