

$$7. y = kx^n$$

$$\begin{aligned}\log_5 y &= \log_5 kx^n \\ &= \log_5 k + \log_5 x^n\end{aligned}$$

$$\log_5 y = \log_5 k + n \log_5 x$$

$$y = mx + c$$

$$\underline{y = 125x^{-2}}$$

$n = \text{gradient}$

$\log_5 k = y \text{ intercept}$

$$n = \frac{3 - -1}{0 - 2} = \frac{4}{-2} = -2$$

$$\log_5 k = 3$$

$$5^3 = k$$

$$k = 125$$

Question			Generic scheme	Illustrative scheme	Max mark
7.			Method 1 <ul style="list-style-type: none"> •¹ state equation of line •² introduce logs •³ use laws of logs •⁴ use laws of logs •⁵ state k and n 	Method 1 <ul style="list-style-type: none"> •¹ $\log_5 y = -2\log_5 x + 3$ •² $\log_5 y = -2\log_5 x + 3\log_5 5$ •³ $\log_5 y = \log_5 x^{-2} + \log_5 5^3$ •⁴ $\log_5 y = \log_5 5^3 x^{-2}$ •⁵ $k = 125, n = -2$ 	5
			Method 2 <ul style="list-style-type: none"> •¹ state equation of line •² use laws of logs •³ use laws of logs •⁴ use laws of logs •⁵ state k and n 	Method 2 <ul style="list-style-type: none"> •¹ $\log_5 y = -2\log_5 x + 3$ •² $\log_5 y = \log_5 x^{-2} + 3$ •³ $\log_5 \frac{y}{x^{-2}} = 3$ •⁴ $\frac{y}{x^{-2}} = 5^3$ •⁵ $k = 125, n = -2$ 	
			Method 3 <ul style="list-style-type: none"> •¹ introduce logs to $y = kx^n$ •² use laws of logs •³ interpret intercept •⁴ use laws of logs •⁵ interpret gradient 	Method 3 The equations at •¹, •², and •³ must be stated explicitly. <ul style="list-style-type: none"> •¹ $\log_5 y = \log_5 kx^n$ •² $\log_5 y = n\log_5 x + \log_5 k$ •³ $\log_5 k = 3$ •⁴ $k = 125$ •⁵ $n = -2$ 	

Question		Generic scheme	Illustrative scheme	Max mark
7.	(continued)			
		<p>Method 4</p> <ul style="list-style-type: none"> •¹ interpret point on log graph •² convert from log to exponential form •³ interpret point and convert •⁴ substitute into $y = kx^n$ and evaluate k •⁵ substitute other point into $y = kx^n$ and evaluate n 	<p>Method 4</p> <ul style="list-style-type: none"> •¹ $\log_5 x = 0$ and $\log_5 y = 3$ •² $x = 1, y = 5^3$ •³ $\log_5 x = 2$ and $\log_5 y = -1$ $x = 5^2$ and $y = 5^{-1}$ •⁴ $5^3 = k(1)^n \Rightarrow k = 125$ •⁵ $5^{-1} = 5^3 \times 5^{2n}$ $\Rightarrow 3 + 2n = -1$ $\Rightarrow n = -2$ 	
Notes:				
<p>1. In any method, marks may only be awarded within a valid strategy using $y = kx^n$.</p> <p>2. Markers must identify the method which best matches the candidates approach; markers must not mix and match between methods.</p> <p>3. Penalise the omission of base 5 at most once in any method.</p> <p>4. In Method 4, candidates may use (2, -1) for •¹ and •² and (0, 3) for •³.</p> <p>5. Do not accept $k = 5^3$.</p> <p>6. In Method 3, do not accept $m = -2$ or gradient = -2 for •⁵.</p> <p>7. Accept $y = 125x^{-2}$ for •⁵.</p>				
Commonly Observed Responses:				