

$$10. a) P = 4.99087 \left(\frac{\cancel{24.55}}{42.5 - 24.55} \right)^{1.81}$$

$$= 929 \text{ points}$$

$$b) 850 = 0.188807 (600 - 210)^k$$

$$850 = 0.188807 \times 390^k$$

$$4502 = 390^k$$

$$\Rightarrow \log 4502 = \log 390^k$$

$$\log_{390} 4502 = k$$

$$\log 4502 = k \log 390$$

$$k = 1.41$$

$$k = \frac{\log 4502}{\log 390} = \underline{1.41}$$

| Question | | | Generic scheme | Illustrative scheme | Max mark |
|---|-----|--|--|---|----------|
| 10. | (a) | | • ¹ evaluate P for $t = 24.55$ | • ¹ 929 | 1 |
| Notes: | | | | | |
| 1. Accept any answer which rounds 929.0368007... to at least 2 significant figures. | | | | | |
| Commonly Observed Responses: | | | | | |
| | (b) | | • ² substitute for P and D • ³ arrange equation in the form $a = b^k$ • ⁴ write in logarithmic form • ⁵ solve for k | • ² $850 = 0.188807(600 - 210)^k$ • ³ $\frac{850}{0.188807} = (600 - 210)^k$ • ⁴ eg $\ln\left(\frac{850}{0.188807}\right) = \ln(600 - 210)^k$ or $k = \log_{(600-210)} \frac{850}{0.188807}$ • ⁵ 1.41 | 4 |
| Notes: | | | | | |
| 2. • ³ may be implied by • ⁴ . 3. Any base may be used at • ⁴ stage. 4. Accept 1.4 at • ⁵ . 5. The calculation at • ⁵ must follow from the valid use of exponentials and logarithms at • ³ and • ⁴ . See Candidate A. 6. For candidates who take an iterative approach to arrive at the value $t = 1.41$ award 1/4. However, if, in the iterations P is calculated for $t = 1.405$ and $t = 1.415$ then award 4/4. | | | | | |
| Commonly Observed Responses: | | | | | |
| Candidate A - invalid use of exponentials | | | Candidate B - transcription error | | |
| $850 = 0.188807(600 - 210)^k$ • ² ✓ $850 = 73.63473^k$ • ³ ✗ • ⁴ ✗ • ⁵ ✗ $\log_{73.63473} 850 = k$ 1.56... | | | $850 = \underline{0.18807}(600 - 210)^k$ • ² ✗ $4519.59... = 390^k$ • ³ ✓ 1 $\log_{390} 4519.59...$ • ⁴ ✓ 1 1.41... • ⁵ ✓ 1 | | |

[END OF MARKING INSTRUCTIONS]