

$$8. \log_6 x + \log_6 (x+5) = 2\log_6 6$$

$$\log_6 x(x+5) = \log_6 6^2$$

$$x^2 + 5x = 36$$

$$x^2 + 5x - 36 = 0$$

$$(x+9)(x-4)$$

$$x = \cancel{-9} \quad \textcircled{x=4}$$

Question			Generic Scheme	Illustrative Scheme	Max Mark
8.			Method 1 <ul style="list-style-type: none"> •¹ apply $\log_6 x + \log_6 y = \log_6 xy$ •² write in exponential form •³ express in standard quadratic form •⁴ solve quadratic and state solution of log equation 	Method 1 <ul style="list-style-type: none"> •¹ $\log_6 (x(x+5)) = \dots$ •² $x(x+5) = 6^2$ •³ $x^2 + 5x - 36 = 0$ •⁴ $-9, 4$ and $x > 0 \Rightarrow x = 4$ 	4
			Method 2 <ul style="list-style-type: none"> •¹ apply $\log_6 x + \log_6 y = \log_6 xy$ •² apply $m \log_6 x = \log_6 x^m$ •³ express in standard quadratic form •⁴ solve quadratic and state solution of log equation 	Method 2 <ul style="list-style-type: none"> •¹ $\log_6 (x(x+5)) = \dots$ •² $\dots = \log_6 6^2$ •³ $x^2 + 5x - 36 = 0$ •⁴ $-9, 4$ and $x > 0 \Rightarrow x = 4$ 	

Notes:

1. Accept $\log_6 x(x+5) = \dots$ for •¹.
2. •² is not available for $x(x+5) = 2^6$; however candidates may still gain •³ and •⁴.
3. •³ and •⁴ are only available if the quadratic reached at •³ is obtained by applying the rules in •¹ and •².
4. •⁴ is only available for solving a polynomial of degree two or higher.
5. At •⁴, accept any indication that -9 has been discarded. For example, scoring out $x = -9$ or underlining $x = 4$.

Commonly Observed Responses:

Candidate A $\log_6 (x(x+5)) = 2$ $x(x+5) = 12$ $x^2 + 5x - 12 = 0$ $\frac{-5 \pm \sqrt{73}}{2}$ and $x > 0 \Rightarrow x = \frac{-5 + \sqrt{73}}{2}$	<ul style="list-style-type: none"> •¹ ✓ •² ✗ •³ ✓ 1 •⁴ ✓ 1 	Candidate B $\log_6 (x(x+5)) = 2$ $x(x+5) = 64$ $x^2 + 5x - 64 = 0$ $\frac{-5 \pm \sqrt{281}}{2}$ and $x > 0 \Rightarrow x = \frac{-5 + \sqrt{281}}{2}$	<ul style="list-style-type: none"> •¹ ✓ •² ✗ •³ ✓ 1 •⁴ ✓ 1
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