

16 (a)

$P(4, k)$

$C(1, -2)$

$$d = \sqrt{(4-1)^2 + (k-(-2))^2}$$

$$= \sqrt{3^2 + (k+2)^2}$$

$$= \sqrt{9 + k^2 + 4k + 4}$$

$$= \sqrt{k^2 + 4k + 13}$$

(b) radius = 5

$$\sqrt{k^2 + 4k + 13} > 5$$

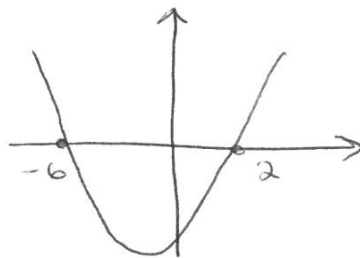
$$k^2 + 4k + 13 > 25$$

$$k^2 + 4k - 12 > 0$$

$$(k + 6)(k - 2)$$

$$k = -6$$

$$k = 2$$



$$k^2 + 4k - 12 > 0$$

when  $k < -6, k > 2$

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Question			Generic scheme	Illustrative scheme	Max mark
16.	(a)		<ul style="list-style-type: none"> <li>•<sup>1</sup> identify centre</li> <li>•<sup>2</sup> apply distance formula and demonstrate result</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>1</sup> (1, -2) stated or implied by •<sup>2</sup></li> <li>•<sup>2</sup> <math>\sqrt{(4-1)^2 + (k-(-2))^2}</math> leading to <math>\sqrt{k^2 + 4k + 13}</math></li> </ul>	2
<b>Notes:</b>					
1. Beware of candidates who ‘fudge’ their working between • <sup>1</sup> and • <sup>2</sup> .					
<b>Commonly Observed Responses:</b>					
	(b)		<ul style="list-style-type: none"> <li>•<sup>3</sup> interpret information</li> <li>•<sup>4</sup> express inequality in standard quadratic form</li> <li>•<sup>5</sup> determine zeros of quadratic expression</li> <li>•<sup>6</sup> state range with justification</li> </ul>	<ul style="list-style-type: none"> <li>•<sup>3</sup> <math>\sqrt{k^2 + 4k + 13} &gt; 5</math></li> <li>•<sup>4</sup> <math>k^2 + 4k - 12 &gt; 0</math></li> <li>•<sup>5</sup> -6, 2</li> <li>•<sup>6</sup> <math>k &lt; -6, k &gt; 2</math> with eg sketch or table of signs</li> </ul>	4
<b>Notes:</b>					
2. Where a candidate has used an incorrect expression from part (a), • <sup>3</sup> is not available. However, • <sup>4</sup> , • <sup>5</sup> and • <sup>6</sup> are still available for dealing with an expression of equivalent difficulty.					
3. Candidates who do not work with an inequation from the outset lose • <sup>3</sup> , • <sup>4</sup> and • <sup>6</sup> . However, • <sup>5</sup> is still available. See Candidate A.					
<b>Commonly Observed Responses:</b>					
<b>Candidate A</b> $\sqrt{k^2 + 4k + 13} = 5$ $k^2 + 4k - 12 = 0$ $k = -6, k = 2$ For P to lie outside the circle $k < -6, k > 2$			<ul style="list-style-type: none"> <li>•<sup>3</sup> ✗</li> <li>•<sup>4</sup> ✗</li> <li>•<sup>5</sup> ✓</li> <li>•<sup>6</sup> ✗</li> </ul>		