

15

(a)

$$\sin 2x + 6 \cos x = 0$$

$$2 \sin x \cos x + 6 \cos x = 0$$

$$2 \cos x (\sin x + 3) = 0$$

$$2 \cos x = 0$$

$$\cos x = 0$$

$$x = 90^\circ, 270^\circ$$

$$\sin x + 3 = 0$$

$$\sin x = -3$$

$$x = \text{No solutions}$$

(b) $\sin 4x + 6 \cos 2x = 0$

$$2x = \overbrace{90^\circ, 270^\circ}^{+360}, 450^\circ, 630^\circ$$

$$x = 45^\circ, 135^\circ, 225^\circ, 315^\circ$$

Question			Generic scheme	Illustrative scheme	Max mark
15.	(a)		<ul style="list-style-type: none"> •¹ substitute appropriate double angle formula •² factorise •³ solve for $\cos x^\circ$ and $\sin x^\circ$ •⁴ solve for x 	<ul style="list-style-type: none"> •¹ $2 \sin x^\circ \cos x^\circ + 6 \cos x^\circ = 0$ •² $2 \cos x^\circ (\sin x^\circ + 3) = 0$ <div> <div>•³</div> <div>•⁴</div> </div> <ul style="list-style-type: none"> •³ $\cos x^\circ = 0$ $\sin x^\circ = -3$ •⁴ $x = 90, 270$ 'no solutions' 	4
Notes:					
<ol style="list-style-type: none"> Do not penalise the absence of '=0' at •¹ and •². Do not penalise the absence of '2' as a common factor at •². Do not penalise the omission of degree signs. Candidates who leave their answer in radians do not gain •⁴ (if marking horizontally) or •³ (if marking vertically). •⁴ is only available if one of the equations at •³ has no solution. Accept $\sin x^\circ = -3$ at •⁴. 					
Commonly Observed Responses:					
Candidate A			Candidate B - insufficient evidence for • ³		
$2 \sin x \cos x = -6 \cos x$ $2 \sin x = -6$ $\sin x = -3$			$2 \sin x^\circ \cos x^\circ + 6 \cos x^\circ = 0$ $2 \cos x^\circ (\sin x^\circ + 3) = 0$ $2 \cos x^\circ = 0, \sin x^\circ = -3$ However, $x = 90, 270, \text{'no solutions'}$		
<ul style="list-style-type: none"> •¹ ✓ •² ^ •³ ^ •⁴ ✓ 1 			<ul style="list-style-type: none"> •¹ ✓ •² ✓ •³ ^ •⁴ ^ •³ ✓ •⁴ ✓ 		
	(b)		• ⁵ state solutions	• ⁵ 45, 135, 225, 315	1
Notes:					
Commonly Observed Responses:					